

Math F251

Midterm 2

Spring 2019

Name: _____

Section: F01 (Rhodes)
 F02 (Bueler)

Rules:

You have 60 minutes to complete the exam.

Partial credit will be awarded, but you must show your work.

No calculators, books, notes, or other aids are permitted.

Circle your final answer to each question where appropriate.

If you need extra space, you can use the back sides of the pages. (Clearly label any work you want graded.)

Turn off anything that might go beep during the exam.

Good luck!

Problem	Possible	Score
1	10	
2	10	
3	10	
4	10	
5	15	
6	15	
7	10	
8	10	
Extra Credit	3	
Total	90	

1. (10 points)

Consider the function

$$f(x) = x - 2 \sin(x).$$

- a. Find the critical number(s) of $f(x)$ on the interval $[0, \pi]$

- b. Find the absolute maximum and absolute minimum values of $f(x)$ on the interval $[0, \pi]$.

2. (10 points)

- a. Find the linearization of $g(x) = \sqrt{x}$ at $a = 4$.

- b. Use your result in part **a.** to approximate $\sqrt{3.9}$.

3. (10 points)

A rectangular photograph whose width is 3 times the height is being enlarged, and the height is increasing at a rate of 2 in/min. How fast is the diagonal of the rectangle increasing when the height is 4 in? Indicate units.

4. (10 pts.)

Evaluate the following limits.

a. $\lim_{x \rightarrow \infty} \frac{\ln x}{\sqrt{x}}$

b. $\lim_{\theta \rightarrow \pi/2} \frac{1 - \sin \theta}{1 + \cos(2\theta)}$

Problem 5 continued....

d. Find all points of inflection.

e. Sketch the graph, labeling all important points.

6. (15 points)

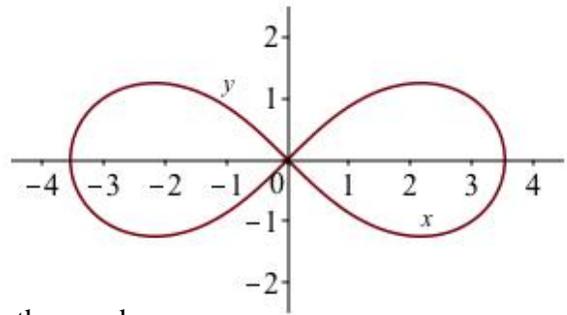
An open-topped box with a square base is to be made so that its volume is 4000 cm^3 . Find the dimensions of the box using the least materials. Indicate units.

7. (10 pts.)

A racetrack is described by the equation

$$2(x^2 + y^2)^2 = 25(x^2 - y^2),$$

whose graph is shown. If an object falls off a speeding car as it travels over the track, it will follow a tangent line.



a. Verify that $(3, 1)$ is a point on the track, and mark it on the graph.

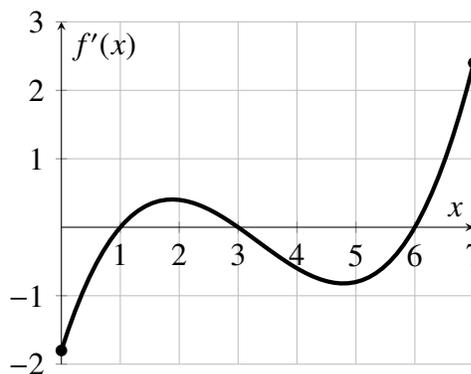
b. Draw the tangent line at $(3, 1)$ on the graph.

c. Find an equation of the tangent line at $(3, 1)$.

8. (10 points)

The graph of the derivative f' of a function f is shown.

- a. On what intervals is f increasing or decreasing? Use interval notation.



- b. At what values of x does f have a local maximum or minimum?

Extra Credit. (3 points)

For $x > 0$, let $g(x) = x^x$. Compute the first and second derivatives of g .