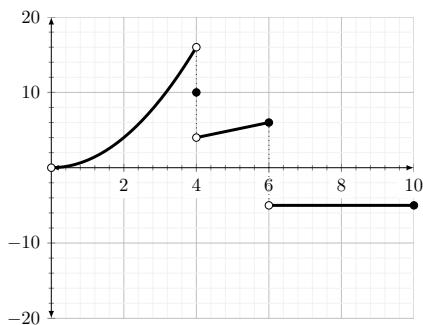


## LECTURE NOTES: §2.2

1. The function  $f(x)$  is graphed below. Use the graph to fill in the blanks.



(a)  $\lim_{x \rightarrow 4^-} f(x) =$  \_\_\_\_\_

(b)  $\lim_{x \rightarrow 4^+} f(x) =$  \_\_\_\_\_

(c)  $\lim_{x \rightarrow 4} f(x) =$  \_\_\_\_\_

(d)  $f(4) =$  \_\_\_\_\_

(e)  $\lim_{x \rightarrow 6^-} f(x) =$  \_\_\_\_\_

(f)  $\lim_{x \rightarrow 6^+} f(x) =$  \_\_\_\_\_

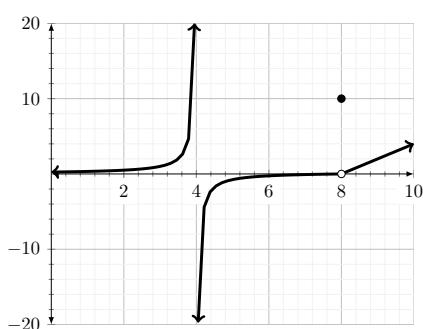
(g)  $\lim_{x \rightarrow 6} f(x) =$  \_\_\_\_\_

(h)  $f(6) =$  \_\_\_\_\_

(i)  $\lim_{x \rightarrow 8} f(x) =$  \_\_\_\_\_

(j)  $f(8) =$  \_\_\_\_\_

2. The function  $g(x)$  is graphed below. Use the graph to fill in the blanks.



(a)  $\lim_{x \rightarrow 4^-} g(x) =$  \_\_\_\_\_

(b)  $\lim_{x \rightarrow 4^+} g(x) =$  \_\_\_\_\_

(c)  $\lim_{x \rightarrow 4} g(x) =$  \_\_\_\_\_

(d)  $g(4) =$  \_\_\_\_\_

(e)  $\lim_{x \rightarrow 8} g(x) =$  \_\_\_\_\_

(f)  $g(8) =$  \_\_\_\_\_

Write the equation of any vertical asymptotes:

3. Evaluate the limits below by graphing  $f(x) = \begin{cases} x + 1 & x < 0 \\ x - 1 & 0 \leq x < 2 \\ 1 + \sqrt{x-2} & 2 < x \end{cases}$

(a)  $\lim_{x \rightarrow 0} f(x)$

(b)  $\lim_{x \rightarrow 2} f(x)$

(c) For which values  $a$  does  $\lim_{x \rightarrow a} f(x)$  exist?

4. Use a calculator and a table of values to determine the limit:  $\lim_{x \rightarrow 0^+} \left( \frac{1}{x} - \ln(x) \right)$ .

5. Sketch the graph of an example of a function  $f$  that satisfies *all* of the given conditions.

(a)  $\lim_{x \rightarrow 0} f(x) = 1$

(b)  $\lim_{x \rightarrow 3^-} f(x) = -2$

(c)  $\lim_{x \rightarrow 3^+} f(x) = 4$

(d)  $f(0) = 2$

(e)  $f(3) = 1$

(f)  $\lim_{x \rightarrow -1^+} f(x) = \infty$