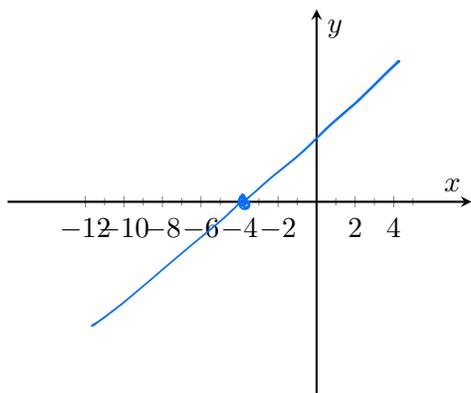
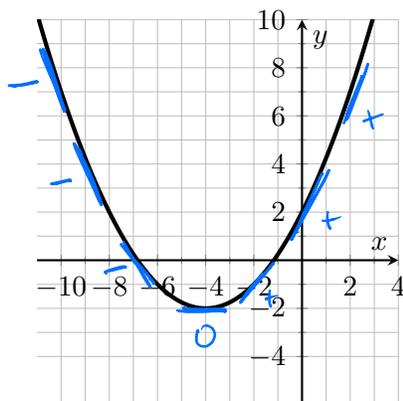


## WORKSHEET §2.8

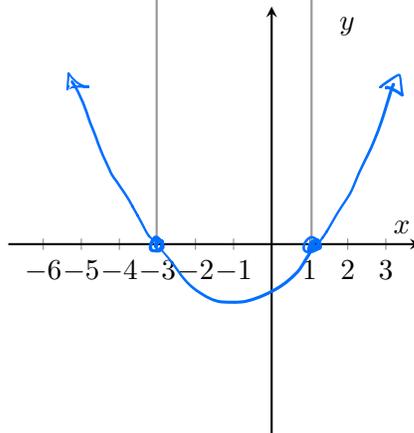
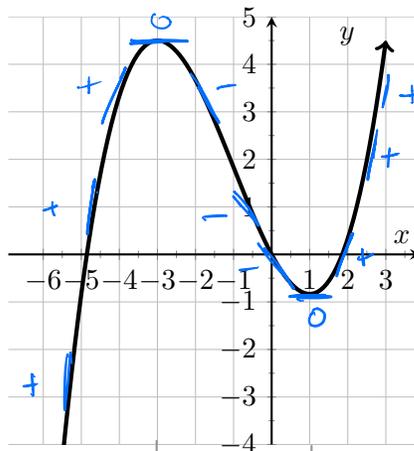
When you are asked to sketch the derivative on the provided axes, I am interested in the qualitative behavior of the derivative: Where does it cross the  $x$ -axis? Is it positive or negative? Is it a lot positive or a little positive? Are the slopes growing steeper or getting less steep? (This is why the  $y$ -axis is unmarked on the answer graphs.)

**Exercise 1.** Sketch the derivatives of the following graphs.

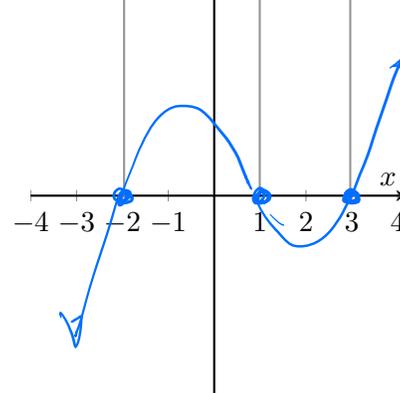
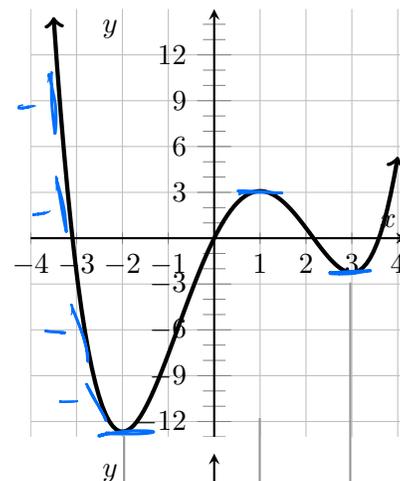
Graph 1



Graph 2



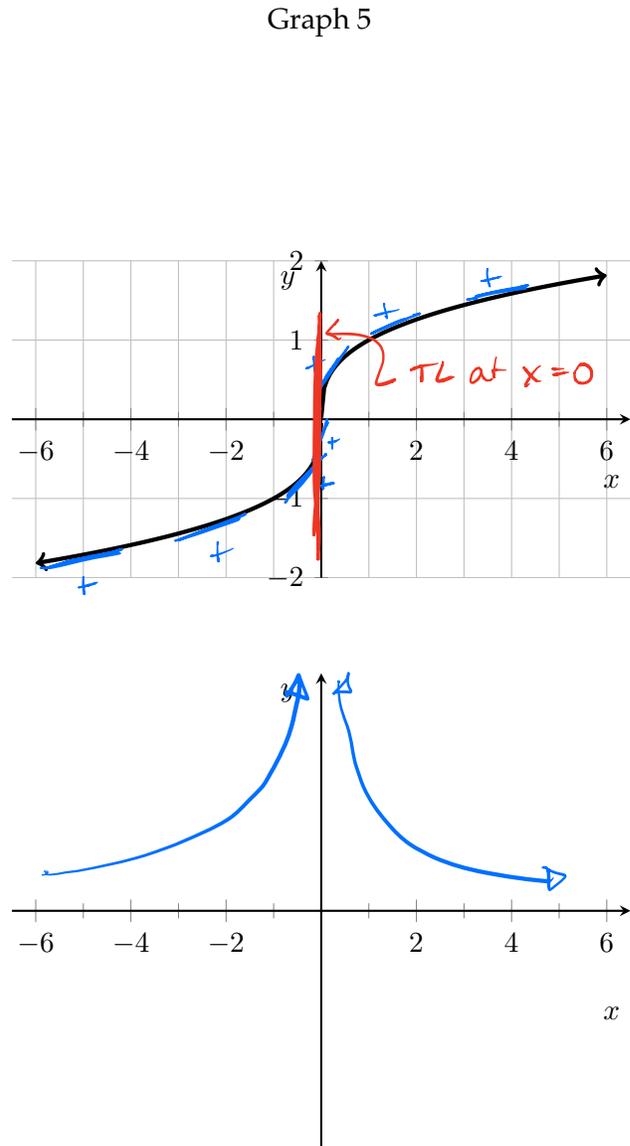
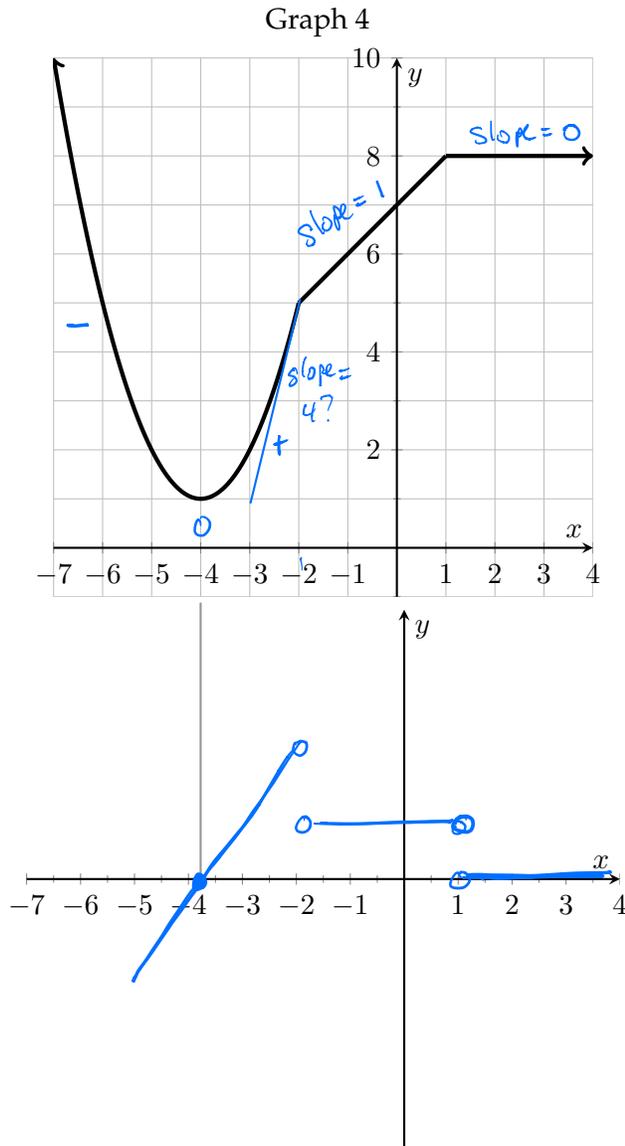
Graph 3



**Exercise 2.** Each of the graphs in Exercise 1 are polynomials. Fill in the blanks:

- Graph 1 looks like a quadratic polynomial (the degree is 2) and the derivative of graph 1 looks like a linear polynomial (the degree is 1).
- Graph 2 looks like a cubic polynomial (the degree is 3) and the derivative of graph 2 looks like a quadratic polynomial (the degree is 2).
- Graph 3 looks like a quartic polynomial (the degree is 4) and the derivative of graph 3 looks like a cubic polynomial (the degree is 3).
- Make a guess:** If  $f(x)$  is a degree  $n$  polynomial, then  $f'(x)$  is a degree  $n-1$  polynomial.

**Exercise 3.** Sketch the derivatives of graphs 4 and 5.



**Exercise 4.** What is an important difference between the derivative of graph 3 (from Exercise 1) and the derivative of graph 4? Use terminology from calculus.

*The derivative of graph 4 is not continuous*

**Exercise 5.** Explain why Graph 5 has a tangent line at  $x = 0$ , even though the derivative is undefined at  $x = 0$ .

*The tangent line at 0 is vertical, so the slope (= derivative) is undefined. As the TL approach 0, their slopes increase w/o bound (they get closer to vertical).*