

Circle your Instructor: Faudree, Williams, Zirbes \_\_\_\_\_ / 15

Name: Solutions

This is a 30 minute quiz. There are 15 problems. Books, notes, calculators or any other aids are prohibited. Calculators and notes are not allowed. **Your answers should be simplified unless otherwise stated.** They should begin  $y' =$  or  $f'(x) =$  or  $dy/dx =$ , etc. There is no partial credit. If you have any questions, please raise your hand.

Circle your final answer.

For each function below, find the derivative.

$$1. g(x) = 2x^{4.3} - \sqrt{2x} + \frac{e}{2} = 2x^{4.3} - \sqrt{2}x^{\frac{1}{2}} + \frac{e}{2}$$

$$\bullet g'(x) = 8.6x^{3.3} - \frac{\sqrt{2}}{2}x^{-\frac{1}{2}}$$

$$\bullet g'(x) = 8.6x^{3.3} - \frac{\sqrt{2}}{2\sqrt{x}}$$

$$\bullet g'(x) = 8.6x^{3.3} - \frac{1}{\sqrt{2x}}$$

$$2. f(x) = \csc(4x) + 3^x$$

$$f'(x) = -4 \csc(4x) \cot(4x) + (\ln 3) 3^x$$

$$3. F(\theta) = 6\theta \tan(\theta)$$

$$F'(\theta) = 6(1 \cdot \tan\theta + \theta \cdot \sec^2\theta) = 6(\tan\theta + \theta \sec^2\theta)$$

or

$$F'(\theta) = 6\tan\theta + 6\theta \sec^2\theta$$

4.  $F(x) = \frac{e^x}{1-x+x^2}$  (Use the Quotient Rule.)

$$\begin{aligned} F'(x) &= \frac{(1-x+x^2)e^x - e^x(-1+2x)}{(1-x+x^2)^2} = \frac{e^x(1-x+x^2+1-2x)}{(1-x+x^2)^2} \\ &= \frac{e^x(x^2-3x+2)}{(1-x+x^2)^2} \text{ or } \frac{e^x(x-2)(x-1)}{(1-x+x^2)^2} \end{aligned}$$

either  
OK.

5.  $h(x) = (4x+1)(2-x)^5$

$$h'(x) = 4\underline{(2-x)^5} + (4x+1) \cdot 5\underline{(2-x)^4}(-1) = \underline{(2-x)^4} [4(2-x) - 5(4x+1)]$$

So  $\boxed{h'(x) = -3(2-x)^4(8x-1)}$

aside calculation  
 $8-4x-20x-5$   
 $=-24x+3$   
 $=-3(8x-1)$

6.  $y = \frac{\sqrt{6}}{5} + \frac{1}{5x} - \frac{x}{3} = \frac{\sqrt{6}}{5} + \frac{1}{5}x^{-1} - \frac{1}{3}x$

$\boxed{y' = -\frac{1}{5}x^{-2} - \frac{1}{3}}$

or  $\boxed{y' = \frac{-1}{5x^2} - \frac{1}{3}}$  or  $\boxed{y' = \frac{-3-5x^2}{15x^2}}$

7.  $y = \frac{-9}{\sqrt{x^2+4}} = -9(x^2+4)^{-\frac{1}{2}}$

$$y' = -9\left(\frac{-1}{2}\right)(x^2+4)^{-\frac{3}{2}}(2x) = +9x(x^2+4)^{-\frac{3}{2}}$$

or  $\frac{9x}{(x^2+4)^{\frac{3}{2}}}$

either  
OK.

Quotient rule is not a good idea!

$$8. z = \frac{t^3 - 7t + 2}{\sqrt{t}} = t^{\frac{5}{2}} - 7t^{\frac{1}{2}} + 2t^{-\frac{1}{2}}$$

$$z' = \frac{5}{2}t^{\frac{3}{2}} - \frac{7}{2}t^{-\frac{1}{2}} - t^{-\frac{3}{2}}$$

$$\text{or } z' = \frac{5}{2}t^{\frac{3}{2}} - \frac{7}{2\sqrt{t}} - \frac{1}{t^{\frac{3}{2}}}$$

$$9. h(x) = x(\ln x)(\cos x)$$

$$\begin{aligned} h'(x) &= 1 \cdot (\ln x)(\cos x) + x \left[ \frac{1}{x} \cdot \cos x + (\ln x)(-\sin x) \right] \\ &= (\ln x)(\cos x) + \cos x - x(\ln x)(\sin x) \end{aligned}$$

$$10. y = 9x^{5/3}(x+2) = 9 \left( x^{\frac{8}{3}} + 2x^{\frac{5}{3}} \right)$$

$$y' = 9 \left[ \frac{8}{3}x^{\frac{5}{3}} + \frac{10}{3}x^{\frac{2}{3}} \right] = 24x^{\frac{5}{3}} + 30x^{\frac{2}{3}} \quad \text{or}$$

$$\underline{y' = 6x^{\frac{2}{3}}(4x+5)}$$

$$11. G(x) = \ln \left( \frac{xe^x}{(x^3+1)^2} \right) = \ln x + \ln e^x - 2 \ln(x^3+1) = \ln x + x - 2 \ln(x^3+1)$$

$$G'(x) = \frac{1}{x} + 1 - 2 \cdot \frac{1}{x^3+1} \cdot 3x^2 = \frac{1}{x} + 1 - \frac{6x^2}{x^3+1} \quad \boxed{\text{or}}$$

$$\underline{G'(x) = \frac{1+x}{x} - \frac{6x^2}{x^3+1}} \quad \text{or } G'(x) = \frac{x^4 - 2x^3 + x + 1}{x(x^3+1)}$$

$$12. g(x) = xe^{1/x} = xe^{x^{-1}}$$

$$\begin{aligned} g'(x) &= 1 \cdot e^{x^{-1}} + x \cdot e^{x^{-1}} \cdot -1x^{-2} \\ &= \underline{e^{x^{-1}}} \left( 1 - \underline{x^{-1}} \right) = \underline{e^{x^{-1}}} \left( 1 - \frac{1}{x} \right) = \underline{e^{x^{-1}}} \left( \frac{x-1}{x} \right) \end{aligned}$$

all OK

13.  $f(x) = (x + \sec(5x))^{-4}$  [You don't need to simplify, but use parentheses correctly.]

$$\begin{aligned} f'(x) &= -4(x + \sec(5x))^{-5} [1 + \sec(5x)\tan(5x) \cdot 5] \quad \leftarrow \text{OK like this.} \\ &= \frac{-4(1 + 5\sec(5x)\tan(5x))}{[x + \sec(5x)]^{-5}} \quad \leftarrow \text{OK} \end{aligned}$$

$$14. H(x) = \arctan(e^{3x})$$

$$H'(x) = \frac{1}{1+(e^{3x})^2} \cdot e^{3x} \cdot 3 = \frac{3e^{3x}}{1+e^{6x}}$$

15. Find  $dA/dt$  for  $A = C \arccos(kt) + 2Ck$  where  $C$  and  $k$  are fixed constants.

$$\frac{dA}{dt} = C \cdot \frac{-1}{\sqrt{1-k^2t^2}} \cdot k = \frac{-Ck}{\sqrt{1-k^2t^2}}$$

or  $\frac{dA}{dt} = \frac{-Ck}{\sqrt{1-(kt)^2}}$