

Below are some principles and/or integration rules you will need for the Integration Proficiency.

1. Integration Rules

(a) $n \neq -1, \int x^n dx =$

(b) $\int \frac{1}{x} dx =$

(c) $\int \sin(x) dx =$

(d) $\int \cos(x) dx =$

(e) $\int \sec^2(x) dx =$

(f) $\int \sec(x)\tan(x) dx =$

(g) $\int e^x dx =$

(h) $\int \frac{1}{1+x^2} dx =$

(i) $\int \frac{1}{\sqrt{1-x^2}} dx =$

2. Each of the following attempts at integration is WRONG. Identify the error and then work the problem correctly.

(a) $\int \frac{3x^2 - 2x}{x^{1/2}} dx = \frac{x^3 - x^2}{(2/3)x^{3/2}} + C$

(b) $\int (x-1)(2x+1) dx = \left(\frac{x^2}{2} - x\right)(x^2 + x) + C$

(c)

$$\int (x + 2x \sin(x^2 + 1)) dx = \int (u + \sin(u)) du = \frac{1}{2}u^2 - \cos(u) + C = \frac{1}{2}(x^2 + 1)^2 - \cos(x^2 + 1) + C$$

$$\text{Let } u = x^2 + 1$$

$$du = (2x)dx$$