

Name: \_\_\_\_\_

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30 minutes maximum. No aids (book, calculator, etc.) are permitted. Show all work and use proper notation for full credit. Answers should be in reasonably-simplified form. 25 points possible.

1. **[7 points]** Find the area of the region in the first quadrant enclosed by  $y = 2 - 2x$ ,  $y = 2 - x^2$ , and the  $x$ -axis. (*Hint: Careful sketch first. Integrating with respect to either  $x$  or  $y$  will work.*)

2. [13 points]

a. Sketch the region bounded by  $y = x^2$ ,  $y = 0$ , and  $x = 1$ .

b. Find the volume of the solid formed by revolving the region in part **a.** around the  $x$ -axis.  
(*Hint: Use discs or washers.*)

- c. Find the volume of the solid formed by revolving the region in part **a.** around the  $y$ -axis.  
(*Hint: Use discs or washers.*)

3. **[5 points]** A solid has a base which is the unit circle in the  $x, y$  plane, and each cross-section parallel to the  $x$ -axis is a square. Find the volume.

**EC. [1 points] (Extra Credit)** Rotating the line  $y = x$ , on the interval  $0 \leq x \leq 1$ , around the  $x$ -axis generates a cone. Find the area of this cone; do not include the area of the “base” of the cone at  $x = 1$ . (*Hint: No need to integrate! Unroll and do geometry!*)

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