Fall 2025

Name: _____

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24 points possible; each part is worth 2 points. No aids (book, notes, calculator, phone, etc.) are permitted. Show all work and use proper notation for full credit. Answers should be in reasonably-simplified form.

1. [12 points] Compute the derivatives of the following functions.

a.
$$f(x) = \cos(ax^2 + b)$$
 for fixed constants b and c

b.
$$f(\theta) = \arcsin(\theta) - 2^{\theta} + \frac{1}{e}$$

c.
$$H(t) = t^{2.4} \ln(2t+1)$$

d.
$$f(x) = 5e^{x/2} + \sin^2(x)$$

$$e. \ h(x) = \frac{x + \sin(x)}{x + \pi}$$

f.
$$h(x) = \frac{1}{5x} + \frac{\sqrt{x}}{10}$$

2. [12 points] Compute the following antiderivatives (indefinite integrals) and definite integrals. Remember that antiderivatives need a "+C".

a.
$$\int \sin(2x) + \sqrt{x} \, dx$$

b.
$$\int (6x-5)^{(1/4)} dx$$

$$\mathbf{c.} \int \frac{\sec^2(x)}{\tan(x)} \, dx$$

d.
$$\int \frac{2x^3 + x^2 - 12}{x^2} \, dx$$

e.
$$\int_{-1}^{0} \frac{x}{(2+x)^2} dx$$

$$f. \int \frac{e^t}{1 + e^{(2t)}} dt$$