

Name: \_\_\_\_\_

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30 minutes maximum. No aids (book, calculator, etc.) are permitted. Show all work and use proper notation for full credit. Answers should be in reasonably-simplified form. 25 points possible.

1. **[5 points]** Find the area of the region between  $y = \sin x$  and  $y = \cos x$  on the interval  $[0, \pi/2]$ . (*Hint: Draw a careful sketch first! You may use symmetry if you want.*)

2. **[15 points]**

- a. Sketch the region bounded by  $y = x^2$ ,  $y = 0$ , and  $x = 1$ . Then sketch the solid of revolution formed by rotating the region around the  $x$ -axis. **Please make your sketches adequately large and clear!**

b. Find the volume of the solid which you sketched in part **a**. (*Hint: Use discs or washers.*)

c. Find the volume of the solid formed by revolving the region in part **a** around the  $y$ -axis. (*Hint: Sketch the solid. Use discs or washers.*)

3. [5 points] A solid has a base which is the unit circle in the  $x, y$  plane, and each cross-section parallel to the  $y$ -axis is a square. Find the volume.

EC. [1 points] (Extra Credit) Give the correct value of the definite integral:

$$\int_{-1}^1 \sqrt{1-x^2} dx.$$

(Hint. There is no requirement to use the fundamental theorem of calculus. What is sought is the correct answer, **with some justification**, which might be a sketch.)

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