

1. In earlier notes, we found seven possible coalitions with players  $P_1$ ,  $P_2$ , and  $P_3$ .
  - (a) List them again below.
  - (b) Suppose the system has a fourth player,  $P_4$ . Determine how many coalitions in this case. Try to answer the question without actually listing all of them.
  - (c) What if there is a fifth player,  $P_5$ ?
  - (d) Make a conjecture about how many coalitions are possible with  $n$  players,  $P_1, P_2, P_3, \dots, P_n$ . How would you argue that your count is correct?
  - (e) What does this suggest about the mechanics of calculating the Banzhaf Power Index for a weighted voting system with a lot of players?

2. What is the Banzhaf Power Index

(a) when there is a dictator

(b) for a dummy player

(c) if all players have an equal number of votes

(d) if player  $P_1$  has double the number of votes as player  $P_2$ ?