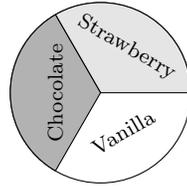


Worksheet 7 (Fair Division 2): The Lone Divider Method

Tom, Fred, and Janet are dividing a super-fancy gourmet cake worth \$36 that is equal parts strawberry, vanilla and chocolate.



$$\frac{36}{3} = \$12$$

- How much value is a fair share of the cake? _____
- Tom divides the cake into three portions (not necessarily according to flavors!) that he values equally. Janet and Fred value the portions according to the following table:

	portion 1	portion 2	portion 3
Tom	\$12	\$12	\$12
Janet	\$7	\$18	\$11
Fred	\$15	\$18	\$3

- Which portion(s) represent a fair share for Janet? portion 2
- Which portion(s) represent a fair share for Fred? portion 1, portion 2
- Is it possible to distribute the portions of cake to the three people so that everyone gets a portion that is a fair share for them? If so, explain how to do so; if not, explain what happens next.

Yes. One distribution: Tom: P₃, Janet: P₂, Fred: P₁

- It turns out that Janet and Fred changed their mind on how they value the portions of cake that Tom gave. Their new values are given in the following table:

	portion 1	portion 2	portion 3
Tom	\$12	\$12	\$12
Janet	\$6	\$20	\$10
Fred	\$7	\$18	\$11

- Which portion(s) represent a fair share for Janet? p2
- Which portion(s) represent a fair share for Fred? p2
- Is it possible to distribute the portions of cake to the three people so that everyone gets a piece that is a fair share for them? If so, explain how to do so; if not, explain what happens next. *No!*

Tom gets P₁. We recombine P₂ and P₃. Janet and Fred proceed w/ Divider-Chooser on recombined cake.

4. In a final cake scenario, suppose that Tom was the lone divider, and the people valued the cake as follows:

- Tom likes all three flavors equally.
- Janet likes strawberry twice as much as vanilla. She likes chocolate SIX times as much as vanilla.
- Fred's values are listed in the table.

trial and error:

V	C	S	
1	6	2	= 9
4	24	8	= 36

multiply by 4

(a) If Tom portioned the cake into three pieces where each piece was a single flavor, determine the valuations that Janet would assign to the pieces of cake (fill in the table).

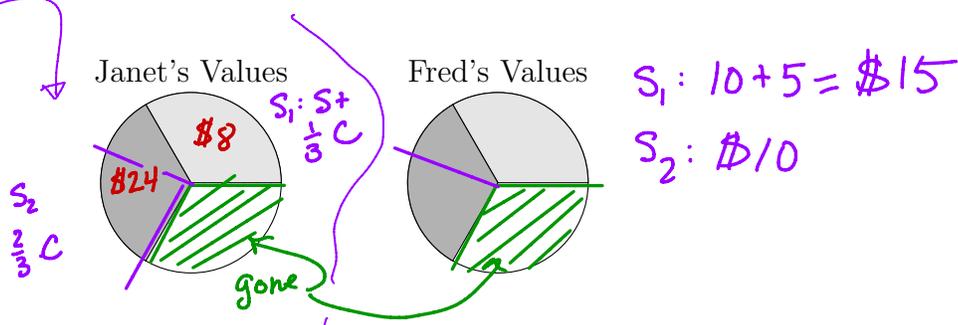
	vanilla	chocolate	strawberry
Tom	\$12	\$12	\$12
Janet	\$4	\$24	\$8
Fred	\$11	\$15	\$10

- (b) Which pieces represent a fair share for Janet? Chocolate
- (c) Which pieces represent a fair share for Fred? chocolate
- (d) Explain why it is not possible to distribute Tom's pieces of cake so that everyone gets a fair share. Chocolate is contested. It's the only piece Janet and Fred perceive as fair.
- (e) Choose a piece of cake to assign to Tom, and explain why you chose that piece. Tom gets vanilla.
- (f) Now, use Divider-Chooser to determine the division of the rest of the cake. Suppose that you flipped a coin, and Janet was chosen to be the divider.
- Label Janet's values on the cake and draw a partition of the cake on Janet's side that Janet might make as the divider. (Don't forget to exclude the part Tom already has!)
 - Label Fred's values and determine the value of Janet's cake division to him.
 - What pieces do Janet and Fred end up with after divider-chooser?

Janet's Calculation

$$\frac{24+8}{2} = \frac{32}{2} = 16$$

$$\frac{2}{3} \cdot \text{Choc} = \frac{2}{3} \cdot \$24 = \$16$$

$$\text{Straw.} + \frac{1}{3} \text{Choc} = 8 + \frac{1}{3} \cdot 24 = \$16$$


Final Outcome: Tom gets V worth \$12, Janet gets $\frac{2}{3}C$ worth \$16, Fred gets S plus $\frac{1}{3}C$ worth \$15.